
THE UNDERLYING SOURCE OF CALCULUS OF FUNCTIONS AND ITS APPLICATIONS TO SOLVEDIVERGENT PROBLEMS.

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Abstract: *Calculus functions in real world are employed to study of rates of change. Before the development of calculus of functions, this couldn't be possible to calculate or study or calculate the objects in motion. However calculus was employed to study and calculate the static objects only and that too should be perfectly static also. Nothing in this universe is perfectly static so calculus of functions has played an unbelievable role in the real world with respect to mathematics, physics or statistics. Let us take an example of objects like a star up to smallest particles of matter doesn't remain in static position. Thus by analyzing the precedent discussion it is good to say that nothing in the universe exists in complete static position. The underlying concept of calculus functions are used to determine how particles or objects from visible range to invisible range like stars, protons, electrons etc move and change with the passage of time.*

In this paper an introductory knowledge related to calculus functions is presented. Moreover the underlying principle of functions and their applicability is discussed and presented predominantly to mathematical field.

1. INTRODUCTION

Calculus functions in real world are employed to study of rates of change. Before the development of calculus of functions, this couldn't be possible to calculate or study or calculate the objects in motion. However calculus was employed to study and calculate the static objects only and that too should be perfectly static also. Nothing in this universe is perfectly static so calculus of functions has played an unbelievable role in the real world with respect to mathematics, physics or statistics. Let us take an example of objects like a star up to smallest particles of matter doesn't remain in static position. Thus by analyzing the precedent discussion it is good to say that nothing in the universe exists in complete static position. The underlying concept of calculus functions are used to determine how particles or objects from visible range to invisible range like stars, protons, electrons etc move and change with the passage of time.

Calculus concepts are not limited to specific fields only however it is applied to different fields such as space science, atomic science, engineering, medical science, statistics, economics and so on. The development of calculus was developed in 17th century by G. Leibniz and Newton. Newton developed concepts of calculus before Leibniz and employed to physical systems. Like Newton, Leibniz also contributed notations to calculus independently. Here the very basic operations are used to employ calculus operations like plus(+), minus(-), division(/) and times(*). calculus practices procedures that service purposes and integrals to estimate rates of alteration or change. In this research paper a preliminary awareness associated to calculus functions is accessible. Moreover the fundamental standard of functions and their applicability is discussed and presented mainly to mathematical field.

2. PRINCIPLE BEHIND CALCULUS OF FUNCTIONS

Calculus of functions works under various principles such as differentiation, integration etc. Differentiation and integration, limits, functions, and so on are some of the most important aspects of calculus that students study. (1,5) Essential theorem of calculus is a link between the two main divisions of calculus, differential and integral calculus, and they exercise the essential concepts of aggregating infinite classifications and infinite configurations [3]. Engineering, science, and economics all use calculus on a regular basis in the modern world. Differential and Integral calculus are two of the most common types of mathematical calculus.

Differential Calculus Basics: Finding the rate of change with regard to other variables is the focus here. The maxima and minima of a function can be found using derivatives to arrive at the best possible result. The study of a quotient's limit is the foundation of differential calculus. Variables like x and y , functions $f(x)$, and the constant changes in x and y are all part of the deal. Differentials refer to the dy and dx symbols. Finding derivatives is a step in the differentiation process. Derivatives of a function can be expressed as dy/dx or f' if the function is linear (x). When the function is written in this way, it signifies that the function is defined as the $y-x$ derivative. Let's take a closer look at some of the most important aspects of the differential calculus. There was an introduction to the fundamentals of differential and integral calculus. [2] Weierstrass, after a great deal of work, was able to eliminate the indication of a limit. **Limits**

The impending term or the degree of nearness to any value. A limit is generally uttered using the limit formula as-

$$\lim_{x \rightarrow c} f(x) = A \quad \lim_{x \rightarrow c} cf(x) = A$$

It is read as "the limit of f of x as x approaches c equals A ".

Derivatives

Immediate rate of change of a quantity with respect to the other quantity. The derivative of a function is represented as:

$$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = A \quad \lim_{h \rightarrow 0} \frac{hf(x+h) - f(x)h}{h} = A$$

Continuity

A function $f(x)$ is said to be continuous at a particular point $x = a$, if the below three conditions are satisfied –

- $f(a)$ is defined
- $\lim_{x \rightarrow a} f(x) = f(a)$ occurs
- $\lim_{x \rightarrow a} f(x) = f(a)$

Continuity and Differentiability

Continuous function is differentiable at any point, whereas the vice-versa condition is not true always.

The rule of Quotient: As the name suggests, it is used to determine the function's derivative (differentiation).

The rule of chain: The chain-rule is a method for determining the derivative of a function's composition.

Integral Calculus Basics: It's known as integral calculus, and it's all about the characteristics of integrals. determining the following two things:

F 's value may be used to compute F' (i.e. from its derivative). It is defined in the interval of consideration when a f function is differentiable.

In order to calculate the area beneath a curve.

Integration: Differentiation and its inverse, integration, are mutually exclusive concepts. When a portion is implicitly divided into many smaller pieces, integration is the collecting of minor parts in order to make a whole. This is how differentiation and integration are synonymous. Areas are frequently calculated using this formula.

Definite Integral: Calculating a function inside the boundaries of a defined integral is necessary. Definite integrals are used to mark the independent variable's bottom and upper bounds, respectively. As an example, a definite integral is shown as: $\int_a^b f(x).dx = F(x)$.

Indefinite Integral

There is no top or lower limit for an indefinite integral, hence there is no upper or lower limit for an indefinite integral. Consequently, there is always a constant value associated with integration (C). The following is how it's identified: $\int f(x).dx = F(x) + C$

3: Applications of Calculus Functions

Calculus functions give a wide range of applications indissimilar fields. The applications of calculus functions are presented and clarified in connection to different domains;

IndustrialArea:

Calculating Building Resources - Quantity surveyors: Engineers and architects utilise calculus integration to estimate the amount of material needed to complete a building project.

To Calculate the weight of various Structures – The Engineering of Architectural:In engineering, curved constructions like dams, bridges floating in the air, and other structures are analysed using calculus functions. For civil engineering as well as the recovery of some constructions.

Seismic Design (Structural Analysis):In order to govern structural foundations' diverse conformation forces, physical engineers employ mathematics. In order to build earthquake-resistant structures that can withstand any amount of seismic shocks, they use calculus.**To Determine the Structure of Soil:**Calculus functions can be used to calculate the soil's capacity and load-bearing capacity. For multi-faceted enterprises, this helps to stabiliseneighbouring soil pressure and maintain a steady gradient prior to the construction of a physical building.

To Construct Bridges or other similar Structures: Bridges are made up of three main components: the beam, compression members, and tension components. Connecting the coasts, the beam is The rudiments of the services stand-in on the beam are computed using calculus. Traffic, pedestrians and other loads will be included in this calculation. While building a beam, the application of calculus helps to choose which material to utilise. The following is a list of similar engineering applications:

To Design Drains for Storm

- Analysis of Hydraulic Programs
- Space Examination (Space Engineering)
- Geometry (Analytical)
- Algebraic

OrganicArea:

- **The Progression of Bacterial Growth:** Differential calculus is used by biologist to estimate the precise growth rate of bacteria under various conditions, such as temperature and food supply. " Using logistics differential equations and exponential equations, the rate of bacterial growth may be determined.

- **Diagnostic of Diseases:** The pace at which a patient becomes ill or recovers is estimated by doctors. An accurate assessment of the prognosis can lead to harmful circumstances and assist choose suitable action. Calculus is a useful tool for predicting and calculating these changes."
- **Epidemiology – Calculate the rate of disease spread:** This is employed to calculate the intensity of spread of different diseases.
- **To Determine the Cardiac Problems:** One further application of calculus is to estimate the heart's total work output, or TWOT. With the use of a dye, the rate of blood flow through the heart may be calculated.
- **Cancer Monitoring and Detection:** To quantify the development or shrinking of a tumour, as well as the overall number of cells present, calculus is applied. Analyzing the disease's development or reversal is done using an exponential function.
- Similar other applications in the medical field are given as under;
 - *Surgery (To Control RBCs)*
 - *Anesthesiologists*
 - *Entomologists*

AstronomyArea:

Physicists use integration calculus in many areas e.g. to calculate the center of mass, the center of gravity, mass moment of inertia and many other applications.

- **To calculate center of mass:** The location of an object's or system's centre of mass may be determined mathematically. It's the average of the system's components. They are weighed based on their mass. The centroid is the centre of mass of all rigid objects with homogeneous densities. A ring's centre of mass may be calculated using calculus, as there is no material in the centre.
- **To Calculate Gravity using its Central Point:** Gravity is imposed on an item from the location where its centre of gravity is located. Center of mass and centre of gravity are same in a uniformly distributed gravitational field.
- **Inertia (Sports, Vehicles etc.):** The moment of inertia is an object's confrontation to alteration in its rotating motion. Inertia is continuously restrained by a orientation line the axis of revolution. Inertia is the amount of confrontation that a figure of a certain mass when lacking in gesture or stationary from touching. Inertia calculates the struggle of the object to battle change. For example, weightier substances have trouble in hastening and trouble in discontinuing. This here, is employed to compute the moment of inertia due to its comfort of use in incessant variables.
- **Calculate Velocity of an object:** Calculus uses Newton's second and third laws of motion to calculate the orbital velocity of a rocket around the earth and its ability to

escape the earth's gravitational pull. The thrust of a rocket into space is based on the calculus of motion.

- **Calculate the Trajectory of an object:** This is employed to compute the route of a rocket. As the rocket propellant burns the rocket involvements exciting acceleration. The retrograde thrust applies a push power on the missile in the conflicting direction, uphill. The change of impetus which is the first imitative of momentum is calculated using calculus.
- **Predict positions of planets:** Calculus is employed in astronomy to discovery out the rate at which planets change over time. The terrestrial laws of wave are used by astronomers to revision planet orbits consequent by using calculus. Since the 17th-century calculus has been used to accurately calculate the variable speed of moving the planet in space and their orbits around stars in equal time.

Investigation Specialists

- **Considering variables in the manufacturing:** Calculus is used by researchers to analyse manufacturing processes to estimate operational efficiency, production, and profitability.
- **Evaluate survey data:** In order to achieve more accurate forecasts and take the proper action, statisticians utilise calculus to estimate survey data that includes numerous dissimilar queries with a wide range of possible replies. In order to determine the total area of the ground surface, land surveyors use a variety of methods, including measuring air, water, and other elements, such as power lines and sewer lines. Calculus is used to solve variables in the surface area calculation.
- **Calculating birth and death rates:** Calculus is used by population ecologists to describe population dynamics that represent growth without environmental restrictions Birth and death rates can be utilised to correctly estimate population shifts and the future.

Commercial Area

- **Credit card payments:** Calculus is used by credit card companies to set payment structures, they consider different variables such as changing interest rates and fluctuating balances to calculate the minimum amount due on a credit card.
- **To Plan Prosecution Cases:** Lawyers use calculus to build the discipline necessary to solve complex problems while prosecuting cases.
- **Calculate costs:** Economists use calculus to calculate the costs of production.

- **To Calculate Revenue:** While expanding output, it is possible to compute an increase in income through the application of calculus. Because of this, the businessman can optimise earnings by focusing on the rate of production.
- **In the field of Economics:** The price elasticity of demand and supply is calculated using calculus in economics. In order to compute elasticity, the supply-demand curve is taken into account, as well as the price of the product, which affects its elasticity. Calculus helps us solve problems, forecast the future, explore the unknown, and understand our environment and the cosmos."
- **Statistics:**

In very rare cases when integration is used for theoretical concepts. Let us understand this having an example that to find any growing distribution function, we contribute the possibility compactness function. Integrals are all over the place in stats. Differentiation also displays up - e.g. maximum probability comprises the incline. At an actual level, one e.g. of calculus being used in statistics involves assimilating over pieces of a possibility dispersal. This will harvest the growing possibility finished those standards, which is basically comes under the curve area. The unlimited fundamental of the possibility dispersal will harvest a growing dissemination function, which is just a function that profits the accumulative likelihood for a random significance.

Related through additional arcs, we can use the normal calculus methods to catch modulation facts, most, specks, etc. Fundamentally, integrals will take the place of limited calculations when incessant standards are used: for example, "relegating out" values. Calculus is tremendously widespread in additional progressive arithmetical submissions. Frequently, this is the request of a basic idea to an additional multifaceted purpose, though.

Working statisticians in academe all employ calculus regularly and the equally is factual of numerous in administration, business and not-for-profit research organizations. However certain expert statisticians don not use abundant, if any, calculus. We infrequently employ calculus. It motivates the math and apparatuses that are used, but here we have no need to pact straight with that level of mathematical element on a classic day.

4: Conclusion and Future Work.

In this investigation paper a brief summary concerning the calculus functions is provided. In addition of the introduction the main motive which lies behind this paper is that to present the various applications of calculus functions in real life activities and events. The knowledge of calculus functions must be acquired to deal with diverse subject domains so that to tackle and understand the problems in a very lucid and smooth manner.

The application of calculus functions is dominating almost every field of the world whether it is related to mathematical or not. In this paper different application of calculus functions is presented in reference to diverse fields. Thus it would be better to say that to maximize the benefits and positive outcome from diverse fields, the applicability of calculus functions must be there. There is tremendous scope of calculus functions to solve different mathematical or other field related issues with an acceptable solution. So in future different

types of functions whether it is integration or differentiation branch must be applied to different unsolved problems existing in various fields.

5. References

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